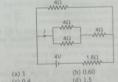
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Engineering Entrance Exam

- The width of the diffraction band varies
 - (a) inversely as the wavelength
 - (b) directly as the width of the slit
 - (c) directly as the distance between the slit and the screen
 - (d) inversely as the size of the source from which the slit is illuminated
- 2. An unpolarised beam of intensity Io is incident on a pair of nicols making an angle of 60° with each other. The intensity of light emerging from the pair is
- 3. A cyclist starts from the centre O of a circular park of radius 1 km, reaches the edge P of the park, then cycles along the circumference and returns to the centre along QO as shown in the figure. If the round trip takes 10 min, the net displacement and average speed of the cyclist (in metre and kilometre
 - (a) 0, 1

 - (d) 0, 21.4
- 4. A beam of light of wavelength 600 nm from a distant source falls on a single slit 1 mm wide and the resulting diffraction pattern is observed on a screen 2m away. The distance between the first dark fringes on either side of the central bright fringe is
 - (a) 1.2 cm
- (b) 1.2 mm (d) 2.4 mm
- 5. The physical quantity having the dimensions $[M^{-1}L^{-3}T^3A^2]$ is

- (d) electromotive force
- 6. A battery of emf 10 V and internal resistance 3Ω is connected to a resistor. The current in the circuit is 0.5 A. The terminal voltage of the battery when the circuit is closed is
 - (a) 10 V
- 7. A galvanometer coil has a resistance of 15 Ω and gives full scale deflection for a current of 4 mA. To convert it to an ammeter of range 0 to
 - (a) 10 m Ω resistance is to be connected in parallel to the galvanometer
 - (b) 10 m Ω resistance is to be connected in series with the galvanometer
 - (c) 0.1Ω resistance is to be connected in
 - (d) 0.1Ω resistance is to be connected in series
- 8. A straight wire of mass 200 g and length 1.5 m carries a current of 2.A. It is suspended in mid air by a uniform horizontal magnetic field B. The magnitude of B (in tesla) is (assume that $g = 9.8 \text{ ms}^{-2}$)
- 9. In the circuit shown the value of I in ampere is



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(a) (1/27) of the original value

(b) (1/9) of the original value

(a) zero (b) half that due to a single charge (c) double that due to a single charge	(c) (1/18) of the original value(d) (1/3) of the original value18. In a transistor the collector current is always
(d) dependent on the position of the dipole t. A parallel plate air capacitor has a capacitance C. When it is half filled with a dielectric of dielectric constant 5, the percentage increases	less than the emitter current because (a) collector side is reverse biased and the emitter side is forward biased (b) a few electrons are lost in the base and only
in the capacitance will be (a) 400% (b) 66.6% (c) 33.3% (d) 200% 2. A comb run through one's dry hair attracts	remaining ones reach the collector (c) collector being reverse biased, attracts less electrons (d) collector side is forward biased and emitter side is reverse biased
small bits of paper. This is due to (a) comb is a good conductor (b) paper is a good conductor (c) the atoms in the paper get polarised by the charged comb (d) the comb possesses magnetic properties (3. The specific charge of a proton is 9.6 × 10 ⁷ C kg ⁻¹ . The specific charge of an an japha particle will be	19. A transparent cube of 0.21 m edge contains a small air bubble. Its apparent distance when viewed through one face of the cube is 0.10 m and when viewed from the opposite face is 0.04 m. The actual distance of the bubble from the second face of the cube is (a) 0.06 m (b) 0.17 m (c) 0.05 m (d) 0.04 m
(a) 9.6 × 10 ⁷ Ckg ⁻¹ (b) 19.2 × 10 ⁷ Ckg ⁻¹ (c) 4.8 × 10 ⁷ Ckg ⁻¹ (d) 2.4 × 10 ⁷ Ckg ⁻¹	20. White light is incident on one of the refracting surfaces of a prism of angle 5°. If the refractive indices for red and blue colours are 1.641 and 1.659 respectively, the angular separation between these two colours when they emerge
14. When light of wavelength 300 nm falls on a photoelectric emitter, photoelectrons are liberated. For another emitter, light of	out of the prism is (a) 0.9° (b) 0.09° (c) 1.8° (d) 1.2°
marelength 600 nm is sufficient for liberating photoelectrons. The ratio of the work function of the two emitters is (a) 1 · 2 (b) 2 · 1 (c) 4 : 1 (b) 2 · 1 (c) 4 : 1 (d) 1 · 4 15. White light is passed through a dilute solution	21. For a given lens, the magnification was found to be twice as large as when the object was 0.15 m distant from it as when the distance was 0.2 m. The focal length of the lens is (a) 1.5 m (b) 0.20 m (c) 0.10 m
of potassium permanganate. The spectrum produced by the emergent light is	22. To a fish under water, viewing obliquely a fisherman standing on the bank of a lake, the

(c) band absorption spectrum (d) line absorption spectrum

(d) line absorption spectrum

(e) the same height as he actually is (d) depends on the obliquity members of the Lyman and Paschen series

23. A thin prism P₁ with angle 4° made fr

respectively, then $\lambda_1: \lambda_2$ is
(a) 1:3 (b) 1:30

(a) 1:3 (b) 1:30 (c) 7:50 (d) 7:108

(a) band emission spectrum

(b) line emission spectrum

The total flux across the sphere is

 Activity of a radioactive sample decreases to (1/3) rd of its original value in 3 days. Then, in 9 days its activity will become 23. A thin prism P₁ with angle 4° made from a glass of refractive index 1.54 is combined with another thin prism P₂ made from glass of refractive index 1.72 to produce dispersion without deviation. The angle of the prism P₂ is

(a) taller than what he actually is

(a) 5.33°

man looks

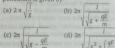
(b) 4°

Unfold Every Question

24. Specific rotation of sugar solution is 0.5 deg m²/kg. 200 kg-m⁻³ of impure sugar solution is taken in a sample polarimeter tube of length 20 cm and optical rotation is found to be 19°. The percentage of purity of sugar is (a) 20% (b) 80%

(d) 89%

25. A simple pendulum has a length land the mass of the bob is m. The bob is given a charge of a coulomb. The pendulum is suspended between the vertical plates of a charged parallel plate capacitor. If E is the electric field strength between the plates, the time period of the



26. A satellite in a circular orbit of radius R has a period of 4 h. Another satellite with orbital radius 3 R around the same planet will have a

(a) 16 (b) 4

- (c) 4√27 (d) 4√8 27. The freezer in a refrigerator is located at the top section so that
 - (a) the entire chamber of the refrigerator is cooled quickly due to convection
 - (b) the motor is not heated (c) the heat gained from the environment is
 - (d) the heat gained from the environment is

28. The unit of Stefan's constant is

(a) Wm⁻²K⁻¹ (b) WmK⁻⁴

(c) $Wm^{-2}K^{-4}$ (d) $Nm^{-2}K^{-4}$

29. A monoatomic gas is suddenly compressed to (1/8) th of its initial volume adiabatically. The ratio of its final pressure to the initial pressure is (Given the ratio of the specific heats of the given gas to be 5/3) (b) 40/3

(a) 32

(d) 8

30. A Carnot engine takes heat from a reservoir at 627°C and rejects heat to a sink at 27°C. Its efficiency will be

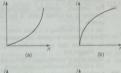
(a) 3/5

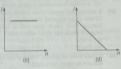
(d) 200/209

31. A 30 V. 90 W lamp is to be operated on a 120 V DC line. For proper glow, a resistor of Ω should be connected in series with the lamp. (b) 10

(d) 30

32. A battery consists of a variable number (n) of identical cells, each having an internal resistance r connected in series. The terminals of the battery are short-circuited. A graph of current (I) in the circuit versus the number of cells will be as shown in figure





33. A tuning fork A produces 4 beat/s with another tuning fork B of frequency 320 Hz. On filing one of the prongs of A, 4 beat/s are again heard frequency of the fork A before filing is

(a) 328 Hz (b) 316 Hz

(c) 324 Hz (d) 320 Hz

34. When the length of the vibrating segment of a sonometer wire is increased by 1%, the percentage change in its frequency is

35. The sprinkling of water reduces slightly the temperature of a closed room because

(a) temperature of water is less than that of the

(b) specific heat of water is high

(c) water has large latent heat of vaporisation

(d) water is a bad conductor of heat

- 36. The equation of a simple harmonic wave is given by $y = 5 \sin \frac{\pi}{2} (100t - x)$, where x and y are in metre and time is in second. The period of the wave in second will be (a) 0.04

37. The loudness and pitch of a sound note depends on (a) intensity and frequency

(b) frequency and number of harmonics (c) intensity and velocity

(d) frequency and velocity

38. For ordinary terrestrial experiments, the observer in an inertial frame in the following cases is

(a) a child revolving in a giant wheel (b) a driver in a sports car moving with a constant high speed of 200 kmh-1 on a straight rod

(c) the pilot of an aeroplane which is taking off (d) a cyclist negotiating a sharp curve

39. A rectangular vessel when full of water, takes 10 min to be emptied through an orifice in its bottom. How much time will it take to be emptied when half filled with water? (b) 7 min (a) 9 min

(d) 3 min (c) 5 min

40. If there were no gravity, which of the following will not be there for a fluid ?

(a) Viscosity (b) Surface tension

(c) Pressure

(d) Archimedes' upward thrust

41. In a LCR series circuit, the potential difference between the terminals of the inductance is 60 V, between the terminals of the capacitor is 30 V and that across the resistance is 40 V. Then, supply voltage will be equal to (b) 70 V (a) 50 V

(d) 10 V (c) 130 V

42. When deuterium and helium are subjected to an accelerating field simultaneously, then (a) both acquire same energy

(b) deuterium accelerates faster (c) helium accelerates faster

- (d) neither of them is accelerated 43. A solenoid 1.5 m long and 0.4 cm in diameter
- possesses 10 turns per cm length. A current of 5 A falls through it. The magnetic field at the axis inside the solenoid is

(a) $2\pi \times 10^{-3}$ T (b) $2\pi \times 10^{-5}$ T

(d) $4\pi \times 10^{-3}$ T (c) $4\pi \times 10^{-2}$ T

- 44. A wire PQR is bent as shown in figure and is placed in a region of uniform magnetic field B. The length of PQ = QR = L A current I ampere flows through the wire as shown. The magnitude of the force on PQ and QR will be (a) BIL 0 (b) 2BIL 0 (c) 0, BII
- (d) 0, 0 45. A choke is preferred to a resistance for limiting current in AC circuit because

(a) choke is cheap

(b) there is no wastage of power (c) choke is compact in size

(d) choke is a good absorber of heat

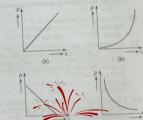
46. To a germanium crystal equal number of aluminium and indium atoms are added. Then (a) it remains an intrinsic semiconductor

(b) it becomes a n-type semiconductor

- (c) it becomes a p-type semiconductor (d) it becomes an insulator
- 47. Maximum velocity of the photoelectrons emitted by a metal surface is 1.2×10⁶ ms⁻¹. Assuming the specific charge of the electron to be 1.8×10^{11} Ckg⁻¹. The value of the stopping potential in volt will be

(c) 4

48. Which of the following figures represents the variation of particle momentum and associated de-Broglie wavelength?



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The term liquid crystal refers to a state that is intermediate between

(c) amorphous liquid and its vapour (d) a crystal immersed in a liquid

50. If r_1 and r_2 are the radii of the atomic nuclei of mass number 64 and 125 respectively, then the ratio (r_1 / r_2) is

Chemistry

Which of the following is not an ore of magnesium?

(a) Carnallite

(b) Dolomite

. The atomic number of Ni and Cu are 28 and 29 respectively. The electronic configuration 1s2, 2s2 2p6, 3s2 3p6 3d10 represents

(a) Cu+ (c) Ni2+

3. In the following, the element with the highest ionisation energy is

(a) $[Ne] 3s^2 3p^1$ (b) $[Ne] 3s^2 3p^3$ (c) [Ne] $3s^2 3p^2$

(d) [Ne] $3s^2 3p^4$

4. In the conversion of Br2 to BrO3, the oxidation number of Br changes from

(a) zero to +5

(b) +1 to +5 (c) zero to -3 (d) +2 to +5

5. Among the alkali metals cesium is the most reactive because

(a) its incomplete shell is nearest to the

(b) it has a single electron in the valence shell (c) it is the heaviest alkali metal

(d) the outermost electron is more loosely bound than the outermost electron of the other alkali metals

6. Which of the following represents the Lewis structure of N2 molecule?

(a) ${}_{\times}^{\times}N = N_{\times}^{\times}$ (b) ${}_{\times}^{\times}N = N_{\times}^{\times}$

7. Hydrogen bond is strongest in

(a) S—H···O (b) O—H···S (d) O - H ··· N (c) F - H ... F 8. The decomposition of a certain mass of CaCO 3

gave 11.2 dm3 of CO2 gas at STP. The mass of KOH required to completely neutralise the gas

(b) 28 g (a) 56 g (d) 20 g (c) 42 g

9. The density of a gas is 1.964 g dm⁻³ at 273 K and 76 cm Hg. The gas is

(d) Xe

 0.06 mole of KNO₃ solid is added to 100 cm³ of water at 298 K. The enthalpy-of KNO3 aqueous solution is 35.8 kJ mol-1. After the solute is dissolved the temperature of the

(c) 301 K

11. 4 moles each of SO2 and O2 gases are allowed to react to form SO3 in a closed vessel. At equilibrium 25% of O2 is used up. The total number of moles of all the gases at equilibrium

An example for autocatalysis is

(a) oxidation of NO to NO2 (b) oxidation of SO2 to SO3

(c) decomposition of KClO3 to KCl and O2 (d) oxidation of oxalic acid by acidified

13. During the fusion of an organic compound with sodium metal, nitrogen of the compound is

14. Identify the product Y in the following reaction sequence

CH2-CH2-COO-CH2-CH2-COO

(b) cyclobutane (d) cyclopentanone

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- 15. The reaction C₂H₅ONa + C₂H₅I → C₂H₅OC₂H₅ + Nal is known as
 (a) Kolbe's synthesis
 - (a) Kolbe's synthesis(b) Wurtz's synthesis
 - (c) Williamson's synthesis
 - (d) Grignard's synthesis
- Glucose contains in addition to aldehyde group
 (a) one secondary OH and four primary OH
 - (b) one primary OH and four secondary OH groups
 - (c) two primary OH and three secondary OH.
 - (d) three primary OH and two secondary OH groups

 17. Which of the following taking place in the blast
- furnace is endothermic?

 (a) $CaCO_3 \longrightarrow CaO + CO_2$

(b) $2C + O_2 \longrightarrow 2CO$ (c) $C + O_2 \longrightarrow CO_2$

(c) $C + O_2 \longrightarrow CO_2$ (d) $Fe_2O_3 + 3CO \longrightarrow 2Fe + 3CO_2$

- 18. The formula mass of Mohr's salt is 392. The iron present in it is oxidised by KMnO₄ in acid medium. The equivalent mass of Mohr's salt is

 (a) 392 (b) 31.6

 (c) 278 (d) 156
- (c) 278 (d) 136

 19. Which of the following solutions will exhibit
 - highest boiling point?
 (a) 0.01 M Na₂SO₄(aq)
 (b) 0.01 M KNO₃(aq)
 - (c) 0.015 M urea (aq) (d) 0.015 M glucose (aq)
- 20. The highest magnetic moment is shown by the transition metal ion with the configuration

(a) $3d^2$ (b) $3d^5$ (c) $3d^7$ (d) $3d^9$

- 21. A transition metal ion exists in its highest oxidation state. It is expected to behave as
 - (a) a chelating agent
 (b) a central metal in a coordination

(c) an oxidising agent (d) a reducing agent

22. In which of the following complex ion, the central metal ion is in a state of sp³d² hybridisation?

(a) [CoFe]³ (b) [Co(NH₃)₄]³⁺

(a) $[CoF_6]^{3-}$ (b) $[Co(NH_3)_6]^{3-}$ (c) $[Fe(CN)_6]^{3-}$ (d) $[Cr(NH_3)_6]^{3+}$

23. Which of the following can participate in

(a) NO₂

(b) H₂ NCH₂CH₂ NH₂

(d):NH₃

24. Which of the following has the highest bond

(a) N₂ (b) O₂

(c) He₂ (d) H₂

25. Which of the following is diamagnetic?

(c) Li₂ (d) He[±]₂

26. The concentration of a reactant X decreases from 0.1 M to 0.005 M in 40 min. If the reaction follows first order kinetics, the rate of the reaction when the concentration of X is 0.01 M

will be (a) $1.73 \times 10^{-4} \text{ M min}^{-1}$

(b) $3.47 \times 10^{-4} \text{ M min}^{-1}$

(c) $3.47 \times 10^{-5} \text{ M min}^{-1}$

(d) 7.5×10^{-4} M min⁻¹

27. Chemical reactions with very high E_a values are generally

(a) very fast (b) very slow (c) moderately fast (d) spontaneous 28. Which of the following does not conduct

(a) Fused NaCl (b) Solid NaCl (c) Brine solution

(d) Copper

29. When a quantity of electricity is passed through CuSO 4 solution, 0.16 g of copper gets deposited. If the same quantity of electricity is passed through acidulated water, then the

[given: atomic weight of Cu = 64]
(a) 4.0 cc
(b) 56 cc

(a) 4.0 cc (b) 56 cc (c) 604 cc (d) 8.0 cc

30. Solubility product of a salt AB is 1 × 10⁻⁸ M² in a solution in which the concentration of A⁺ ions is 10⁻³ M. The salt will precipitate when the concentration of B⁻ ions is kept
(a) between 10⁻⁸ M to 10⁻⁷ M

(b) between 10^{-7} M to 10^{-8} M (c) > 10^{-5} M

c) > 10⁻⁸M

 $(d) < 10^{-8} M$

31. Which one of the following conditions will increase the voltage of the cell represented by the equation ?

 $Cu(s) + 2Ag^{+}(ag) \longrightarrow Cu^{2+}(ag) + 2Ag(s)$

- (a) Increase in the dimension of Cu electrode (b) Increase in the dimension of Ag electrode (c) Increase in the concentration of Cu2+ ions
 - (d) Increase in the concentration of Ag+ ions
- 32. The pH of 10⁻⁸ M HCl solution is

(a) 8

(b) more than 8

- (c) between 6 and 7
- 33. The mass of glucose that should be dissolved in 50 g of water in order to produce the same lowering of pressure as is produced by dissolving 1 g of urea in the same quantity of water is

(d) 18 g

- 34. Osmotic pressure observed when benzoic acid is dissolved in benzene is less than that expected from theoretical considerations. This is because
 - (a) benzoic acid is an organic solute (b) benzoic acid has higher molar mass than
 - (c) benzoic acid gets associated in benzene
- (d) benzoic acid gets dissociated in benzene 35. For a reaction to be spontaneous at all
- temperatures
 - (a) ΔG and ΔH should be negative
 - (b) ΔG and ΔH should be positive (c) $\Delta G = \Delta S = 0$
 - (d) $\Delta H < \Delta G$
- 36. Which of the following electrolyte will have maximum flocculation value for Fe(OH)2 sol? (b) Na₂S (a) NaCl

(c) (NH₄)₃PO₄ (d) K₂SO₄ 37. For a reversible reaction

- $X(g) + 3Y(g) \Longrightarrow 2Z(g)$; $\Delta H = -40 \text{ kJ}$, the standard entropies of X, Y and Z are 60, 40 and 50 JK⁻¹ mol⁻¹ respectively. The temperature at which the above reaction attains equilibrium is about (b) 500 K
 - (a) 400 K (d) 373 K (c) 273 K
- 38. The radii of Na+ and Cl- ions are 95 pm and 181 pm respectively. The edge length of NaCl unit cell is

(a) 276 pm (b) 138 pm (c) 552 pm (d) 415 pm

39. Inductive effect involves

(a) displacement of σ-electrons (b) delocalisation of π-electrons

(c) delocalisation of σ-electrons

40. The basicity of aniline is less than that of

(a) +R effect of -NH2 group (b) -I effect of -NH2 group (c) -R effect of -NH2 group (d) hyperconjugation effect

41. Methyl bromide is converted into ethane by (a) Al (b) Zn

(c) Na (d) Cu

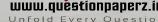
42. Which of the following compound is expected to be optically active? (a) (CH2) CHCHO (b) CH3CH2CH2CHO

(c) CH3CH2CHBrCHO (d) CH3CH2CBr2CHO 43. Which cycloalkane has the lowest heat of

- combustion per CH2 group ? (a) Cyclopropane (b) Cyclobutane (c) Cyclopentane (d) Cyclohexane
- 44. The catalyst used in the preparation of an alkyl chloride by the action of dry HCl on an alcohol (a) anhydrous AlCl₃ (b) FeCl₃ (c) anhydrous ZnCl2 (d) Cu
- 45. In the reaction,

Alcoholic KCN The product B is

- (a) alkyl chloride (c) carboxylic acid
- 46. Which of the following compound would not solution? (a) Salicylic acid
- (d) 4-nitrobenzoic acid (c) Benzoic acid 47. By heating phenol with chloroform in alkali, it is converted into
 - (a) salicylic acid (b) salicylaldehyo (c) anisole



When a mixture of calcium benzoate and calcium acetate is dry distilled, the resulting compound is

- (a) acetophenone (b) benzaldehyde (c) benzophenone (d) acetaldehyde
- Which one of the following does not give benzoic acid on hydrolysis?
- (a) Phenyl cyanide (b) Benzoyl chloride (c) Benzyl chloride (d) Methyl benzoate
- 50. Which of the following would undergo Hofmann reaction to give a primary amine?

Mathematics

- If $(p \land \neg r) \rightarrow (\neg p \lor q)$ is false, then the truth values of p, q and r are respectively (b) F, F and T
- (a) T, F and F (c) F, T and T
- (d) T, F and T
- 2. If α, β and γ are the roots of equation $x^3 - 8x + 8 = 0$, then $\Sigma \alpha^2$ and $\Sigma \frac{1}{\alpha \beta}$

(a) 0 and - 16

- (c) -16 and 0
- (b) 16 and 8 (d) 16 and 0
- 3. The GCD of 1080 and 675 is
 - (b) 135
 - (a) 145 (d) 125
- 4. If a, b and $c \in N$, then which one of the following is not true? (a) $a \mid b$ and $a \mid c \Rightarrow a \mid 3b + 2c$
 - (b) $a \mid b$ and $b \mid c \Rightarrow a \mid c$
 - (c) $a \mid (b+c) \Rightarrow a \mid b$ and $a \mid c$
 - (d) $a \mid b$ and $a \mid c \Rightarrow a \mid b + c$
- 5. $x = 4(1 + \cos \theta)$ and $y = 3(1 + \sin \theta)$ are the parametric equations of

- (d) $\frac{(x-4)^2}{16} + \frac{(y-3)^2}{9} = 1$
- 6. If the distance between the foci and the distance between the directrices of the hyperbola $\frac{x^2}{x^2} - \frac{y^2}{b^2} = 1$ are in the ratio 3: 2,

then a: b is (a) $\sqrt{2:1}$

- 7. The ellipse $\frac{x^2}{25} + \frac{y^2}{16} = 1$ and the hyperbola $\frac{x^2}{25} - \frac{y^2}{16} = 1$ have in common
 - (a) centre only
 - (b) centre, foci and directrices
 - (c) centre, foci and vertices (d) centre and vertices only
- and $\tan \theta = n$, 8. If $\sec \theta = m$
- $\left[(m+n) + \frac{1}{(m+n)} \right]$ is (a) 2 (b) 2m (d) mn (c) 2n
- The value of $\frac{\sin 85^{\circ} \sin 35^{\circ}}{\cos 65^{\circ}}$ is
 - (c) 1 (d) 0
- 10. If the length of the tangent from any point on the circle $(x-3)^2 + (y+2)^2 = 5r^2$ to the circle $(x-3)^2 + (y+2)^2 = r^2$ is 16 unit, then the area between the two circles in sq unit is
 - (a) 32 π (c) 8n
- 11. The equation of the common tangent of the two touching circles, $y^2 + x^2 - 6x - 12y + 37 = 0$ $x^2 + y^2 - 6y + 7 = 0$ is
 - (a) x + y 5 = 0 (b) x y + 5 = 0(c) x-y-5=0 (d) x+y+5=0
 - 12. The equation of the parabola with vertex at
 - (a) $y^2 2y 12x 11 = 0$
 - (b) $x^2 + 2x 12y + 13 = 0$ (c) $y^2 - 2y + 12x + 11 = 0$
 - (d) $y^2 2y 12x + 13 = 0$

- 3. The equation of the line which is tangent to both the circle $x^2 + y^2 = 5$ and the parabola $y^2 = 40x$ is
 - (a) $2x y \pm 5 = 0$
 - (b) 2x y + 5 = 0
 - (c) 2x y 5 = 0(d) 2x + y + 5 = 0
- 4. If $2A + 3B = \begin{bmatrix} 2 & -1 & 4 \\ 3 & 2 & 4 \end{bmatrix}$ and
 - $A + 2B = \begin{bmatrix} 5 & 0 & 3 \\ 1 & 6 & 2 \end{bmatrix}$, then B is (a) $\begin{bmatrix} 8 & -1 & 2 \\ -1 & 10 & -1 \end{bmatrix}$ (b) $\begin{bmatrix} 8 & 1 & 2 \\ 1 & 10 & 2 \end{bmatrix}$
 - (a) $\begin{bmatrix} 8 & -1 & 2 \\ -1 & 10 & -1 \end{bmatrix}$ (b) $\begin{bmatrix} 8 & 1 & 2 \\ -1 & 10 & -1 \end{bmatrix}$ (c) $\begin{bmatrix} 8 & 1 & 2 \\ -1 & 10 & -1 \end{bmatrix}$ (d) $\begin{bmatrix} 8 & 1 & 2 \\ 1 & 10 & 1 \end{bmatrix}$
- 5. If $A = \begin{bmatrix} 1 & -3 \\ 2 & k \end{bmatrix}$ and $A^2 4A + 10I = A$, then k is equal to
 - (a) 0 (c) 4 and not 1
 - (b) -4 (d) 1 or 4
- 6. The value of $\begin{vmatrix} x+y & y+z & z+x \\ x & y & z \\ x-y & y-z & z-x \end{vmatrix}$ is equal to
 - (a) $2(x + y + z)^2$ (b) $2(x + y + z)^3$ (c) $(x + y + z)^3$ (d) 0
- On the set Q of all rational numbers the operation * which is both associative and commutative is given by a* b, is
 - (a) a + b + ab(c) ab + 1
- (b) $a^2 + b^2$ (d) 2a + 3b
- 8. From an aeroplane flying, vertically above a horizontal road, the angles of depression of two consecutive stopes on the same side of the aeroplane are observed to be 30° and 60° respectively. The height at which the aeroplane is flying in km is
 - (a) $\frac{4}{\sqrt{3}}$ (b) $\frac{\sqrt{3}}{2}$
 - (c) $\frac{2}{\sqrt{3}}$ (d) 2
- **9.** If the angles of a triangle are in the ratio 3:4:5, then the sides are in the ratio (a) $2:\sqrt{5}:\sqrt{3}+1$ (b) $\sqrt{2}:\sqrt{6}:\sqrt{3}+1$ (c) $2:\sqrt{3}:\sqrt{3}+1$ (d) 3:4:5
- (c) $2: \sqrt{3} \cdot \sqrt{3} + 1$ (d) 3: 4: 5 **0.** If $\cos^{-1} x = a$, (0 < x < 1) and $\sin^{-1}(2x\sqrt{1-x^2}) + \sec^{-1}\left(\frac{1}{2x^2-1}\right) = \frac{2\pi}{3}$,
 - than $tan^{-1}(2x)$ equals

- (a) $\frac{\pi}{6}$ (b) $\frac{\pi}{4}$
- **21.** If a > b > 0, then the value of $\tan^{-1}\left(\frac{a}{b}\right) + \tan^{-1}\left(\frac{a+b}{a-b}\right)$ depends on
 - (a) both a and b (b) b and not a (c) a and not b (d) neither a nor b
- **22.** If $A = \{a, b, c\}$, $B = \{b, c, d\}$ and $C = \{a, d, c\}$, then $(A B) \times (B \cap C)$ is equal to (a) $\{(a, c), (a, d)\}$
- (a) {(a, c), (a, a)} (b) {(a, b), (c, d)} (c) {(c, a), (d, a)}
 - (d) $\{(a, c), (a, d), (b, d)\}$
- **23.** The function $f: X \to Y$ defined by $f(x) = \sin x$ is one-one but not onto, if X and Y are respectively equal to
 - (a) R and R (b) [0, π] and [0
 - (c) $\left[0, \frac{\pi}{2}\right]$ and [-1, 1]
 - (c) $\left[0, \frac{\pi}{2}\right]$ and $\left[-1, 1\right]$
 - (d) $\left[\frac{-\pi}{2}, \frac{\pi}{2}\right]$ and [-1, 1]
- **24.** If $\log_4 2 + \log_4 4 + \log_4 x + \log_4 16 = 6$, then value of x is
 - (a) 64 (b) 4 (c) 8 (d) 32
- **25.** If $S_n = \frac{1}{6 \cdot 11} + \frac{1}{11 \cdot 16} + \frac{1}{16 \cdot 21} + \dots$ to *n* terms, then $6S_n$ equals
 - (a) $\frac{5n-4}{5n+6}$ (b) $\frac{n}{(5n+4)}$
 - (c) $\frac{2n-1}{5n+6}$ (d) $\frac{1}{(5n+6)}$
- **26.** The remainder obtained when $(1!)^2 + (2!)^2 + (3!)^2 + ... + (100!)^2$ is divided
 - by 10² is (b) 28
 - (c) 17 (d) 14
 - **27.** In the group $G = \{1, 5, 7, 11\}$ under multiplication modulo 12, the solution of $7^{-1} \otimes_{12} (x \otimes_{12} 11) = 5$ is equals
 - (a) 5 (b) 1 (c) 7 (d) 11
- **28.** A subset of the additive group of real numbers which is not a subgroup is

 (a) ((0) + (0) + (0) + (0)
 - (a) $(\{0\}, +)$ (b) (Z, +) (c) (N, +) (d) (Q, +)



- 29. If $\vec{p} = \hat{i} + \hat{j}$, $\vec{q} = 4\hat{k} \hat{j}$ and $\vec{r} = \hat{i} + \hat{k}$, then the unit vector in the direction of $3\vec{p} + \vec{q} - 2\vec{r}$ is
 - (a) $\frac{1}{3}(\hat{i} + 2\hat{j} + 2\hat{k})$
 - (b) $\frac{1}{2}(\hat{\mathbf{i}} 2\hat{\mathbf{j}} 2\hat{\mathbf{k}})$
 - $(c)\frac{1}{2}(\hat{\mathbf{i}}-2\hat{\mathbf{j}}+2\hat{\mathbf{k}})$ (d) $\hat{i} + 2\hat{j} + 2\hat{k}$
- 30. If \vec{a} and \vec{b} are the two vectors such that $|\overrightarrow{a}| = 3\sqrt{3}$, $|\overrightarrow{b}| = 4$ and $|\overrightarrow{a} + \overrightarrow{b}| = \sqrt{7}$, then the

angle between \vec{a} and \vec{b} is (a) 120° (d) 150°

(c) 30°

- 31. If \vec{a} is vector perpendicular to both \vec{b} and \vec{c} , then
 - (a) $\overrightarrow{a} + (\overrightarrow{b} + \overrightarrow{c}) = \overrightarrow{0}$
 - (b) $\overrightarrow{a} \times (\overrightarrow{b} + \overrightarrow{c}) = \overrightarrow{0}$
 - $(c) \overrightarrow{a} \times (\overrightarrow{b} \times \overrightarrow{c}) = \overrightarrow{0}$
 - $(d) \overrightarrow{a} \cdot (\overrightarrow{b} \times \overrightarrow{c}) = \overrightarrow{0}$
 - 32. If the area of the parallelogram with \vec{a} and \vec{b} as two adjacent sides is 15 sq unit, then the area of the parallelogram having, $3\vec{a} + 2\vec{b}$ and $\vec{a} + 3\vec{b}$ as two adjacent sides in sq unit is
 - (b) 105 (a) 120 (d) 45 (c) 75
 - **33.** If the lines x + 3y 9 = 0, 4x + by 2 = 0 and 2x - y - 4 = 0 are concurrent, then b equals (a) -5 (b) 5 (d) 0
 - (c) 1 **34.** The equation of the circle having x - y - 2 = 0and x-y+2=0 as two tangents and $x \rightarrow y = 0$ as a diameter is (a) $x^2 + y^2 + 2x - 2y + 1 = 0$
 - (b) $x^2 + y^2 2x + 2y 1 = 0$
 - (c) $x^2 + y^2 = 2$
 - (d) $x^2 + y^2 = 1$
 - 35. A circular sector of perimeter 60 m with maximum area is to be constructed. The radius of the circular arc in metre must be (b) 5 (a) 20
 - (c) 15
- (d) 10

- **36.** $\int \frac{(x^3 + 3x^2 + 3x + 1)}{(x + 1)^5} dx$ is equal to (a) $-\frac{1}{(x+1)} + c$ (b) $\frac{1}{5} \log(x+1) + c$
- (c) $\log(x+1) + c$ (d) $\tan^{-1} x + c$ $\frac{\csc x}{\cos^2(1 + \log \tan \frac{x}{2})} dx$ is equal to 37. [-
 - (a) $\sin^2\left[1 + \log \tan \frac{x}{2}\right] + c$ (b) $\tan 1 + \log \tan \frac{x}{2} + c$
 - (c) $\sec^2 \left[1 + \log \tan \frac{x}{2} \right] + c$
 - (d) $-\tan\left[1+\log\tan\frac{x}{2}\right]+c$

38. The complex number $\frac{(-\sqrt{3}+3i)(1-i)}{(3+\sqrt{3}i)(i)(\sqrt{3}+\sqrt{3}i)}$ when represented in the Argand diagram is

- (a) in the second quadrant
- (b) in the first quadrant
- (c) on the y-axis (imaginary axis) (d) on the x-axis (real axis)
- 39. If $2x = -1 + \sqrt{3}i$, then the value of $(1-x^2+x)^6-(1-x+x^2)^6$ is equal to
- (a) 32 (b) -64 (c) 64 (d) 0
 - **40.** The modulus and amplitude of $(1 + i \sqrt{3})^8$ are respectively
- (a) 256 and $\frac{\pi}{3}$ (b) 256 and $\frac{2\pi}{3}$ (d) 256 and $\frac{8\pi}{3}$ (c) 2 and $\frac{2\pi}{3}$
 - **41.** The value of $\lim_{x \to 0} 5^x 5^{-x}$
 - (a) log 5 (d) 2 log 5 42. Which one of the following is not true always?
 - (a) If f(x) is not continuous at x = a, then it is not differentiable at x = a(b) If f(x) is continuous at x = a, then it is
 - differentiable at x = a
 - (c) If f(x) and g(x) are differentiable at x = a, then f(x) + g(x) is also differentiable at
 - (d) If a function f(x) is continuous at x = a, then $\lim f(x)$ exists

Unfold Every Question

NDRAPRASTHA (Engg) Solved Paper 2007

II

43.' $\int \frac{dx}{k\sqrt{x^6-16}}$ is equal to	47. The solution of the differential equation
$(a) \frac{1}{3} \sec^{-1} \left(\frac{x^3}{4} \right) + c (b) \cosh^{-1} \left(\frac{x^3}{4} \right) + c$ $(c) \frac{1}{12} \sec^{-1} \left(\frac{x^3}{4} \right) + c (d) \sec^{-1} \left(\frac{x^3}{4} \right) + c$	$e^{-x}(y+1) dy + (\cos^2 x + \sin 2x)y dx = 0$ subjected to the condition that $y = 1$ when $x = 0$ is (a) $y + \log y + e^x \cos^2 x = c$ (b) $\log(y+1) + e^x \cos^2 x = 1$
44. If $I_1 = \int_0^{\pi/2} x \sin x dx$ and $I_2 = \int_0^{\pi/2} x \cos x dx$	
$f(x) = 4x^2 - 3x + 1 \text{ and } g(x) = \frac{f(-x)^2 - f(x)^2}{x^2 + 3}$ then $\int_{-2}^2 g(x) dx$ is equal to (a) 64 (b) -48 (c) 0 (d) 24 46. The area enclosed between the paraby $= x^2 - x + 2$ and the line $y = x + 2$ in squequals (a) $\frac{8}{3}$ (b) $\frac{1}{3}$ (c) $\frac{2}{3}$ (d) $\frac{4}{3}$	the rotto of its distance from two fixed point in the plane is always a constant $k(<1)$ is (a) hyperbola (b) ellipse (c) straight line (d) circle 50. The circles $\alpha x^2 + \alpha y^2 + 2g_1 x + 2f_1 y + q = 0$
PHYSICS 3 (d) 4, (d) 5	. (c) 6. (d) 7. (a) 8. (d) 9. (c) 10. (a) 17. (a) 18. (b) 19. (a) 20. (b)
1. (c) 2. (c) 13. (d) 14. (b) 15 11. (b) 12. (c) 13. (c) 24. (c) 25 21. (c) 22. (a) 23. (b) 34. (c) 35	(d) 25. (c) 27. (a) 28. (c) 29. (a) 30. (c) (d) 25. (c) 27. (a) 38. (b) 39. (b) 40. (d) (d) 25. (c) 27. (a) 38. (b) 39. (b) 40. (d) (e) 46. (c) 47. (c) 48. (d) 49. (a) 50. (d)
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